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## THE CONVEX COMBINATIONS OF QUADRATIC OPERATORS ON $S^2$

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Quadratic operators attract the attention of specialists in various fields of mathematics and its applications (see, for example, [2], [3]). We will use the definition and notation of the reference [1]. In [1] on the two-dimensional simplex the following quadratic stochastic operator was studied:  $V_0 : S^2 \rightarrow S^2$ ,  $\{x_0, x_1, x_2\} = \{x'_0, x'_1, x'_2\}$ , where

$$\begin{aligned} x'_0 &= x_1^2 + 2x_0x_2, & x'_2 &= x_0^2 + 2x_1x_2, & x'_1 &= x_1^2 + 2x_0x_2, \\ x'_1 &= x_0^2 + 2x_1x_2, & x'_0 &= x_1^2 + 2x_0x_2, & x'_2 &= x_1^2 + 2x_0x_2. \end{aligned}$$

It is proved that  $(M(1, 0, 0), M(0, 1, 0), M(0, 0, 1), C(1, 1/2, 1/2))$  are fixed points of the operator  $V_0$ .

Note that in [4] by similar studies the following quadratic stochastic operator  $V_1$ :

$$\begin{cases} V_1 : & \begin{aligned} x'_0 &= 1/2x_1^2 + 1/2x_2^2 + 1/2x_1^2 + 2x_1x_2, \\ x'_1 &= 1/2x_1^2 + 1/2x_2^2 + 1/2x_1^2 + 2x_1x_2, \\ x'_2 &= 1/2x_1^2 + 1/2x_2^2 + 1/2x_1^2 + 2x_1x_2, \end{aligned} \\ x_0 &= 1/2x_1^2 + 1/2x_2^2 + 1/2x_1^2 + 2x_1x_2, \end{cases}$$

It is proved that the operator  $V_1$  has a unique fixed point  $C'$ , and it is a regular operator. In the present paper, we shall consider a convex combination of the operators  $V_0$  and  $V_1$

$$V_\lambda : S^2 \rightarrow S^2, \quad V_\lambda = (1-\lambda)V_0 + \lambda V_1, \quad (\theta \leq \lambda \leq 1).$$

It is easy to see that the operator  $V_\lambda$  has the form:

$$\begin{cases} V_\lambda : & \begin{aligned} x'_0 &= (1-2\lambda)/2x_1^2 + \lambda/2x_1^2 + 1/2x_1^2 + 2x_1x_2, \\ x'_1 &= \lambda/2x_1^2 + 1/2x_2^2 + \lambda/2x_1^2 + 2x_1x_2, \\ x'_2 &= \lambda/2x_1^2 + 1/2x_2^2 + (1-2\lambda)/2x_1^2 + 2x_1x_2, \end{aligned} \\ x_0 &= \lambda/2x_1^2 + 1/2x_2^2 + \lambda/2x_1^2 + 2x_1x_2, \end{cases}$$

Obviously, the operator  $V_\lambda$  is also a quadratic stochastic operator.

**Theorem.** For the operator  $V_\lambda$  the following statements are true:

- The operator  $V_\lambda$  has a unique fixed point  $C$  ( $[3, 1/2, 1/2]$ ).
- If  $\lambda = (2 - \sqrt{5})/2$  then the fixed point  $C'$  is a non-hyperbolic point.
- If  $\theta < \lambda < (2 - \sqrt{5})/2$  then the fixed point  $C$  is a repelling point.
- If  $(2 - \sqrt{5})/2 < \lambda < 1$  then  $C'$  is an attractive point.

### References

- Zakharov M.I. On the behavior of trajectories and ergodic hypothesis for quadratic mappings of a simplex. Russ. Math. Surv. 20(9), 265–266 (1975).
- Lopushinskij V.I. Mathematical structures in population genetics. In: Mathematics, vol. 21. Springer, Berlin (1992).
- Zinchenko U.U., Radzivil L.A. On the dynamics of a strictly non-Volterra quadratic stochastic operator on two-dimensional simplex. St. Mat. 20(10), 120–121 (2009).
- Mamatov B.Zh., Sharipova M.Sh. On one quadratic stochastic operator in  $S^2$ . Abstracts of the Republic of Kazakhstan conference "Symmetries, topology and fractals". 201, pages 101–104.